

PRACTICE 3 Exercise 1
COMPUTATIONAL STRUCTURAL MECHANICS AND DYNAMICS
Marcos Boniquet Aparicio

It's chosen a problem type: *Plates*

Material, self weight condition, and constraints are settled.

The material chosen for the unique surface defined by the four sides has the following properties:

$$E=3*10^{10} \text{ Pa}$$

$$\nu=0,2$$

$$\text{Load: } q=1*10^4 \text{ N/m}^2$$

$$\text{thickness}=0,10 \text{ m}$$

θ_x and θ_y are 0 at clamped boundary, as well as z-displacement.

Remember:

Kirchoff

- 1) Middle plane moves only vertically.
- 2) Points along a normal to the middle plane have same vertical displacement.
- 3) σ_z is negligible
- 4) Points along the normals to the middle plane before deformation remain in straight lines also orthogonal to middle plane after deformation.

Reissner-Midlin

Same points, but assumption 4 changes:

- 4) Points along the normals to the middle plane before deformation remain in straight lines **NOT NECESSARILY** orthogonal to middle plane after deformation.

GID:

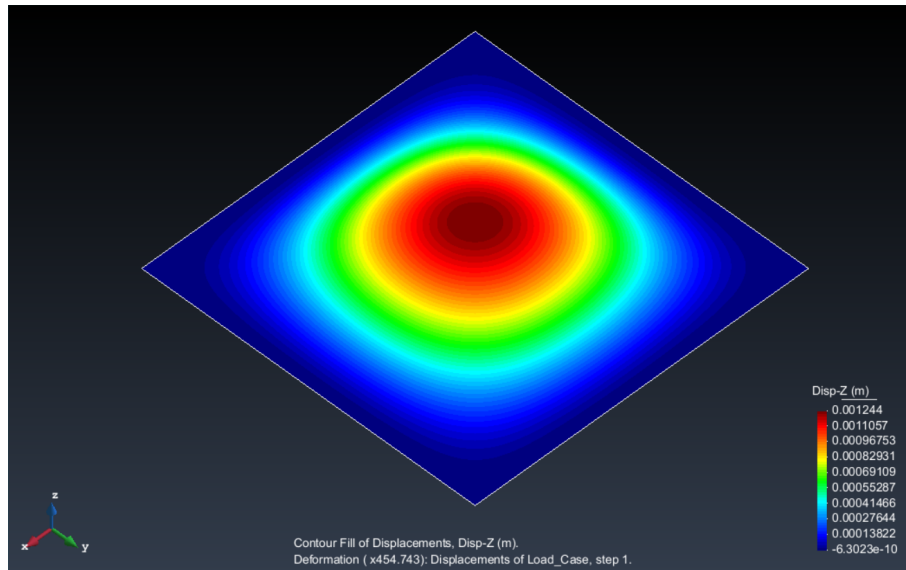
- Linear triangle is DKT triangular
- Quadratic triangle element is R.M
- Linear Quadrilateral element is CLLL

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Triangular linear mesh of 150x150 elements:

Num. of Triangle elements=45000

Num. of nodes=22801



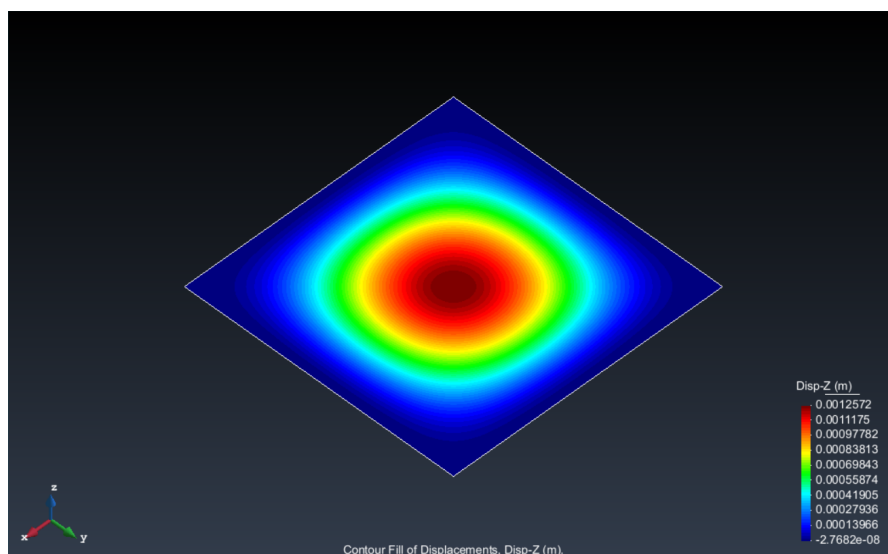
Max. displacement is 1,244mm.

A symmetry with the diagonals (it could be divided in 4 triangular and equal domains) was expected with a linear material behaviour.

With a triangular quadratic mesh, 40x40 elements:

Num. of Triangle elements=3200

Num. of nodes=6561



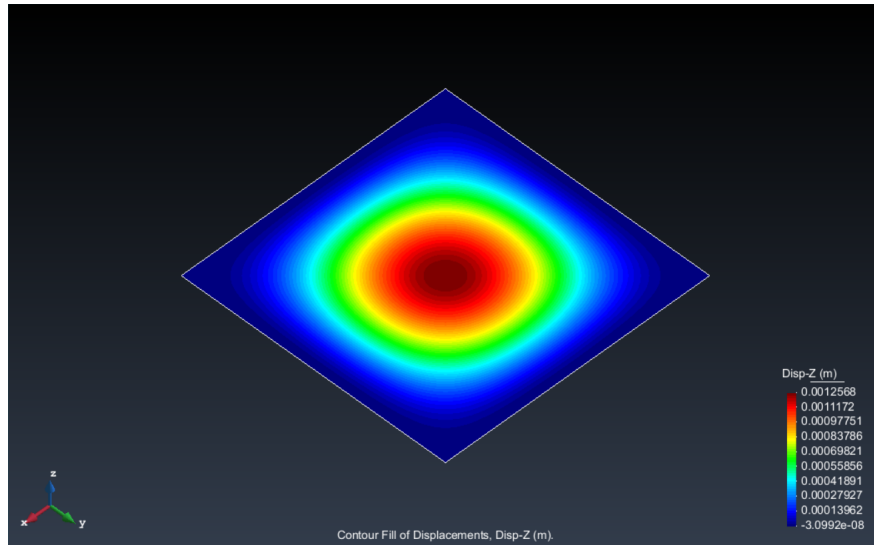
Max. displacement is 1,2572mm.

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With a quadrilateral linear mesh, of 100x100 elements:

Num. of Quadrilateral elements=10000

Num. of nodes=10201



Max. displacement is 1,2568mm.

Analytic result:

$$D = E \cdot t^3 / 12(1 - \nu^2)$$

$$W_{\max} = q \cdot b^4 / 24 \cdot D = 0,0128 \text{ where } b=2, \text{ half of the side of plate.}$$

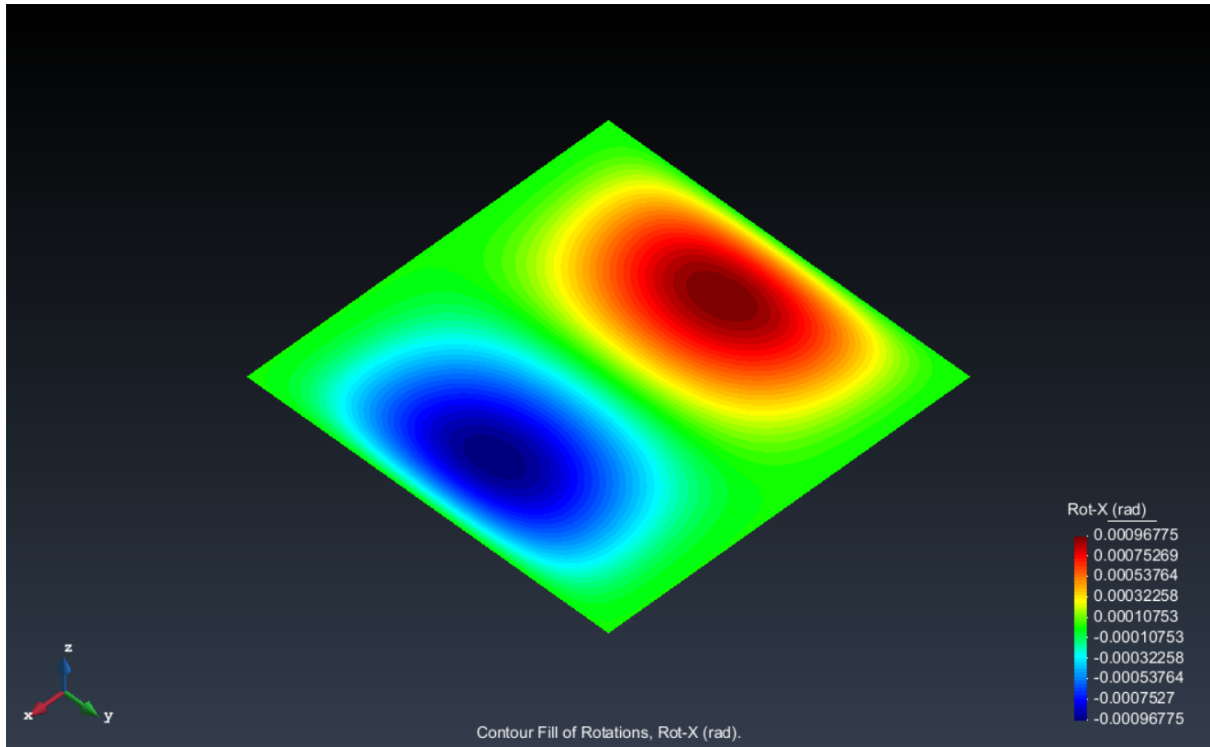
So, comparison between 3 methods and Analytical result:

Linear Triangular	Quadratic Triangular	Linear Quadrilateral	Analytic
1,244	1,2572	1,2568	1,28
97,19%	98,22%	98,19%	

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Rotations:

x-axis



y-axis

